



Receiver-based Recovery of Clipped OFDM Signals for PAPR Reduction: A Bayesian Approach

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Motivation

Bayesian Clipping Recovery

Reliable Carriers as Measurements

Prior Information about clipping

Multiple Antenna Receivers

Multiple User System

Clipped OFDM and Channel Estimation

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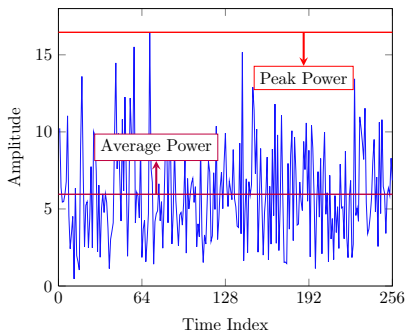
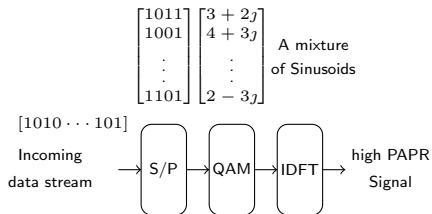
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- ▶ OFDM is a multi-carrier modulation scheme that uses orthogonal carriers.
- ▶ Main Advantages include
 - ▶ Robustness against multi-path fading.
 - ▶ High data rate.
 - ▶ Easy single tap equalization.
- ▶ The main disadvantage is **High PAPR!** [1]



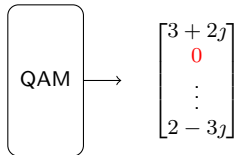
Transmitter based schemes

- ▶ coding, partial transmit sequence (PTS), selected mapping (SLM), interleaving, tone reservation (TR), tone injection (TI) and active constellation extension (ACE).
- ▶ Transmitter-based techniques are complex.

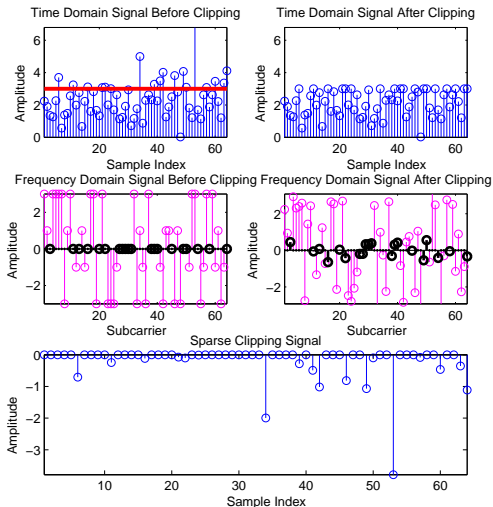
- ▶ We follow a clipping scheme
- ▶ clip signal above a prespecified threshold γ

$$x_p(i) = \begin{cases} \gamma e^{j\angle x(i)} & \text{if } |x(i)| > \gamma \\ x(i) & \text{otherwise} \end{cases}$$

- ▶ $x_p(i) = x(i) + c(i)$



- ▶ Implications:
 - ▶ Clipping signal is **sparse**!
 - ▶ Pilot contamination.
 - ▶ Inter-user Interference.



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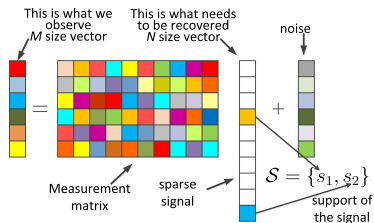


Implications of Sparsity

- ▶ Signal can be reconstructed using sparse signal recovery methods.
- ▶ Few Measurements will be required.

Why Bayesian Recovery?^a

- ▶ Low Complexity.
- ▶ Signal statistics are not required.
- ▶ Agnostic to distribution.
- ▶ Noise statistics are utilized.



^aBy Bayesian recovery, we refer to the utilized SABMP scheme [2].

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- ▶ Reserved tones reduce bandwidth efficiency.
- ▶ Some data carriers (called Reliable tones) can be used as measurements.

Question

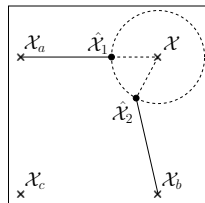
How to select the tones which are most likely to be in their correct decision region?

- ▶ Calculate the metric [3]

$$\mathfrak{R} = \frac{\Pr(\lfloor \hat{\mathcal{X}}(i) \rfloor = \mathcal{X}(i))}{\Pr(\lfloor \hat{\mathcal{X}}(i) \rfloor \neq \mathcal{X}(i))}$$

$\lfloor \cdot \rfloor$ denotes hard decision.

Geometrical representation of adopted reliability criteria.



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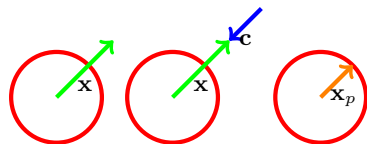
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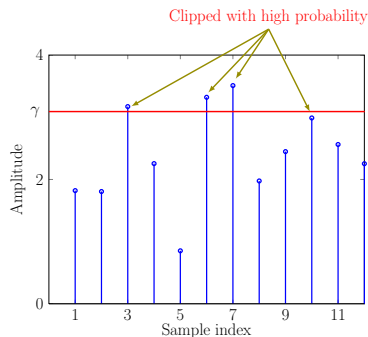
Multiple User System

Clipped OFDM and Channel Estimation

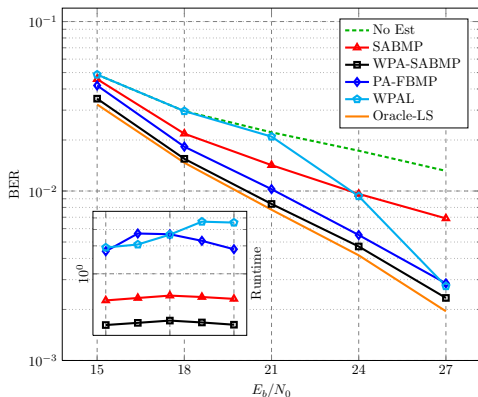
- ▶ Clipping operation does not affect the phase.



- ▶ Phase of the clipping signal can be retrieved from the received clipped signal.
- ▶ This helps in increasing the measurements.



- ▶ Probability of a clipping element is high, if received signal is closer to threshold.
- ▶ Find the dominant support faster and accurately.



Simulation Parameters:

- ▶ Subcarriers: 512
- ▶ QAM Order: 64
- ▶ Reliable Carriers: 128
- ▶ Clipping Ratio: 1.61

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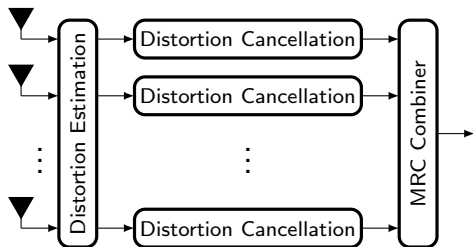
Multiple User System

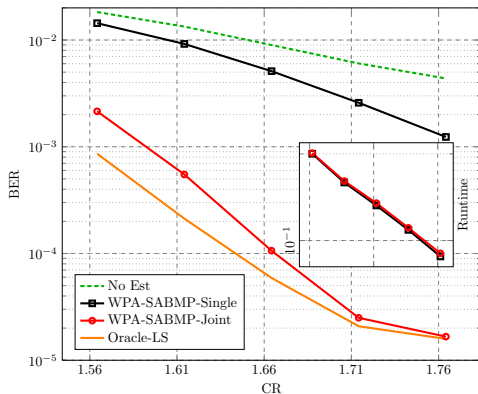
Clipped OFDM and Channel Estimation



- ▶ Multiple receiver antennas provide more measurements for clipping reconstruction.
- ▶ Use measurements from all antennas together to improve clipping mitigation [4].

$$\begin{bmatrix} \bar{\mathbf{y}}_1 \\ \bar{\mathbf{y}}_2 \\ \vdots \\ \bar{\mathbf{y}}_L \end{bmatrix} = \begin{bmatrix} \bar{\Phi}_1 \\ \bar{\Phi}_2 \\ \vdots \\ \bar{\Phi}_L \end{bmatrix} \mathbf{c} + \begin{bmatrix} \bar{\mathbf{z}}_1 \\ \bar{\mathbf{z}}_2 \\ \vdots \\ \bar{\mathbf{z}}_L \end{bmatrix},$$





Simulation Parameters:

- ▶ Subcarriers: 512
- ▶ QAM Order: 64
- ▶ Reliable Carriers: 77
- ▶ E_b/N_0 : 27 dB
- ▶ Antennas: 2

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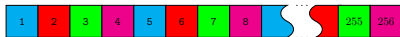
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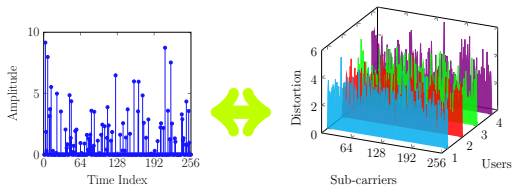
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Orthogonal Channel Allocation

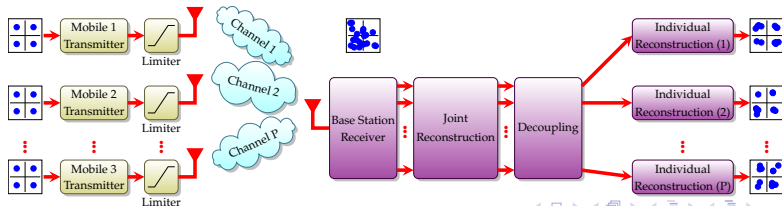


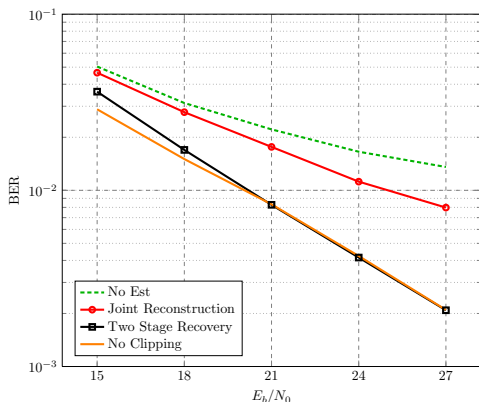
Challenge → Distortions Overlap in Frequency Domain



Two Stage Recovery

- ▶ Initially reconstruct jointly.
- ▶ Form decoupled systems.
- ▶ Perform individual reconstruction.





Simulation Parameters:

- ▶ Subcarriers: 512
- ▶ Users: 2
- ▶ QAM Order: 64
- ▶ Reserved Tones: 75
- ▶ Clipping Ratio: 1.61



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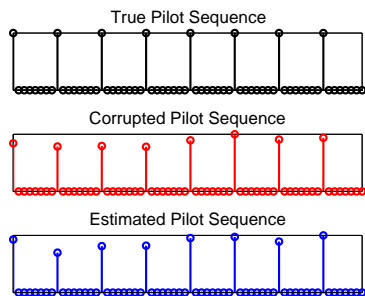
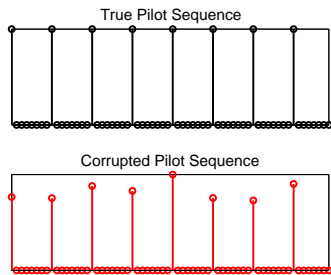
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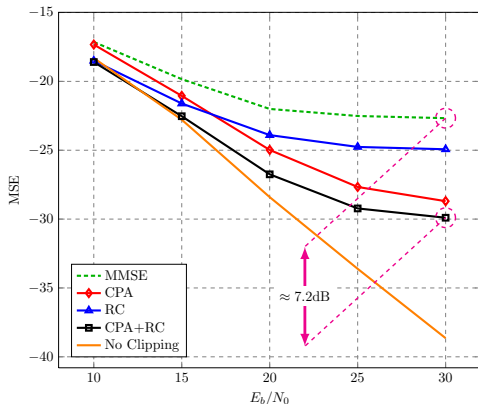


Solutions

- ▶ Increase pilots.
- ▶ Data Aided pilot Estimation.

Proposed

- ▶ Estimate Corrupted Pilots.
- ▶ Use estimated and data aided pilots together.



Simulation Parameters:

- ▶ Subcarriers: 256
- ▶ QAM Order: 64
- ▶ Pilot Tones: 16
- ▶ Reliable Tones: 16
- ▶ Clipping Ratio: 1.73



- [1] S. H. Han and J. H. Lee, An overview of peak-to-average power ratio reduction techniques for multicarrier transmission, *IEEE Wireless Commun.*, vol. 12, no. 2, pp. 5665, 2005.
- [2] M. Masood and T. Y. Al-Naffouri, "Sparse Reconstruction Using Distribution Agnostic Bayesian Matching Pursuit," *IEEE Trans. Signal Process.*, vol. 61, no. 21, pp. 52985309, 2013.
- [3] E. B. Al-Safadi and T. Y. Al-Naffouri, "Pilotless Recovery of Nonlinearly Distorted OFDM Signals by Compressive Sensing over Reliable Data Carriers," in *Proc. IEEE Int. Workshop on Signal Process. Advances in Wireless Commun. (SPAWC)*, 2012.
- [4] A. Ali, A. Al-Zahrani, T. Y. Al-Naffouri, "Receiver Based PAPR Reduction in OFDMA", in *Proc. IEEE Int. Conf. Acoust. Speech Signal Process.*, 2014.

For more information...

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THANK YOU!